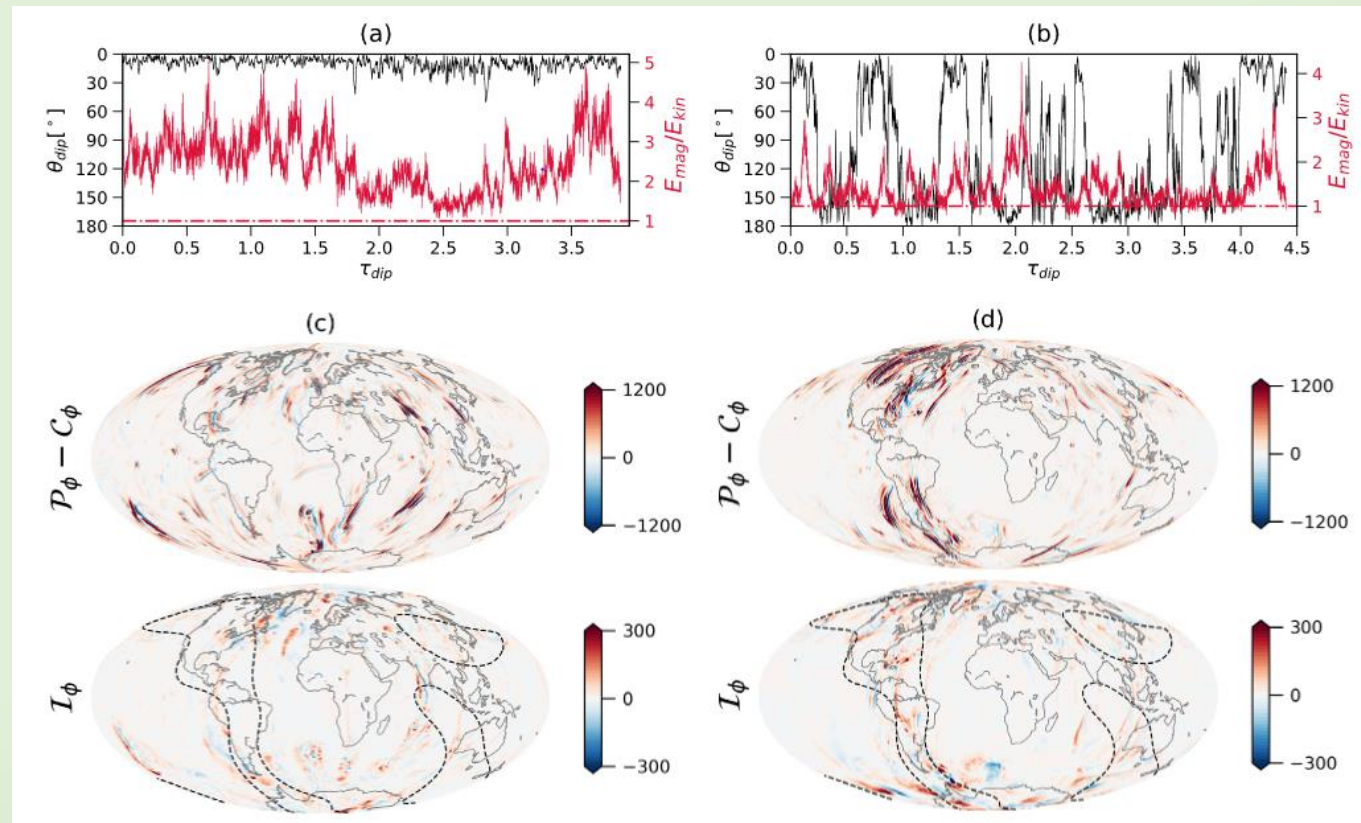


# Dynamo regimes dependence on the heterogeneous CMB heat flux



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Strasbourg, July 2025

## Dynamo models

Non-dimensional MHD equations for an electrically-conductive, Boussinesq, incompressible fluid in a rotating convecting spherical shell (e.g. Olson and Christensen, 2002):

Navier-Stokes (conservation of momentum): 
$$E \left( \frac{\partial \vec{u}}{\partial t} + \vec{u} \cdot \nabla \vec{u} - \nabla^2 \vec{u} \right) + 2\hat{z} \times \vec{u} + \nabla P = Ra \frac{\vec{r}}{R} T + \frac{1}{Pm} (\nabla \times \vec{B}) \times \vec{B}$$

Induction (Maxwell's equations of electromagnetism): 
$$\frac{\partial \vec{B}}{\partial t} = \nabla \times (\vec{u} \times \vec{B}) + \frac{1}{Pm} \nabla^2 \vec{B}$$

Heat (conservation of energy): 
$$\frac{\partial T}{\partial t} + \vec{u} \cdot \nabla T = \frac{1}{Pr} \nabla^2 T$$

Continuity (conservation of mass): 
$$\nabla \cdot \vec{u} = 0$$

No magnetic monopoles: 
$$\nabla \cdot \vec{B} = 0$$

- Thermochemical convection: prescribed CMB flux, fixed ICB temperature, zero co-density sources/sinks.
- No-slip, insulating boundaries.

Heat flux Rayleigh	$Ra = \frac{\alpha g_0 q_0 D^4}{\nu k \kappa}$
Ekman	$E = \frac{\nu}{\Omega D^2}$
Prandtl	$Pr = \frac{\nu}{\kappa}$
magnetic Prandtl	$Pm = \frac{\nu}{\lambda}$

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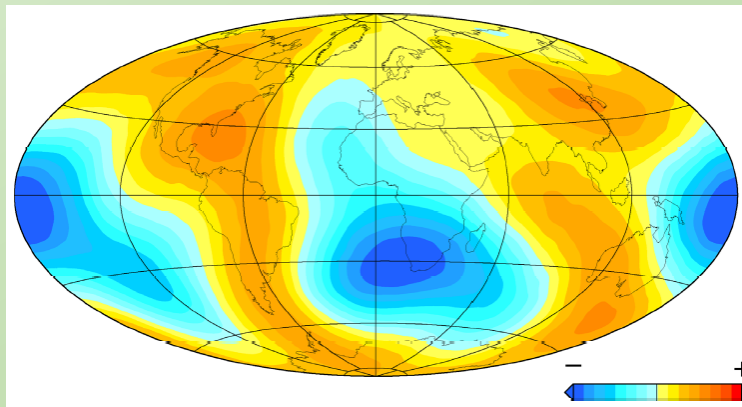
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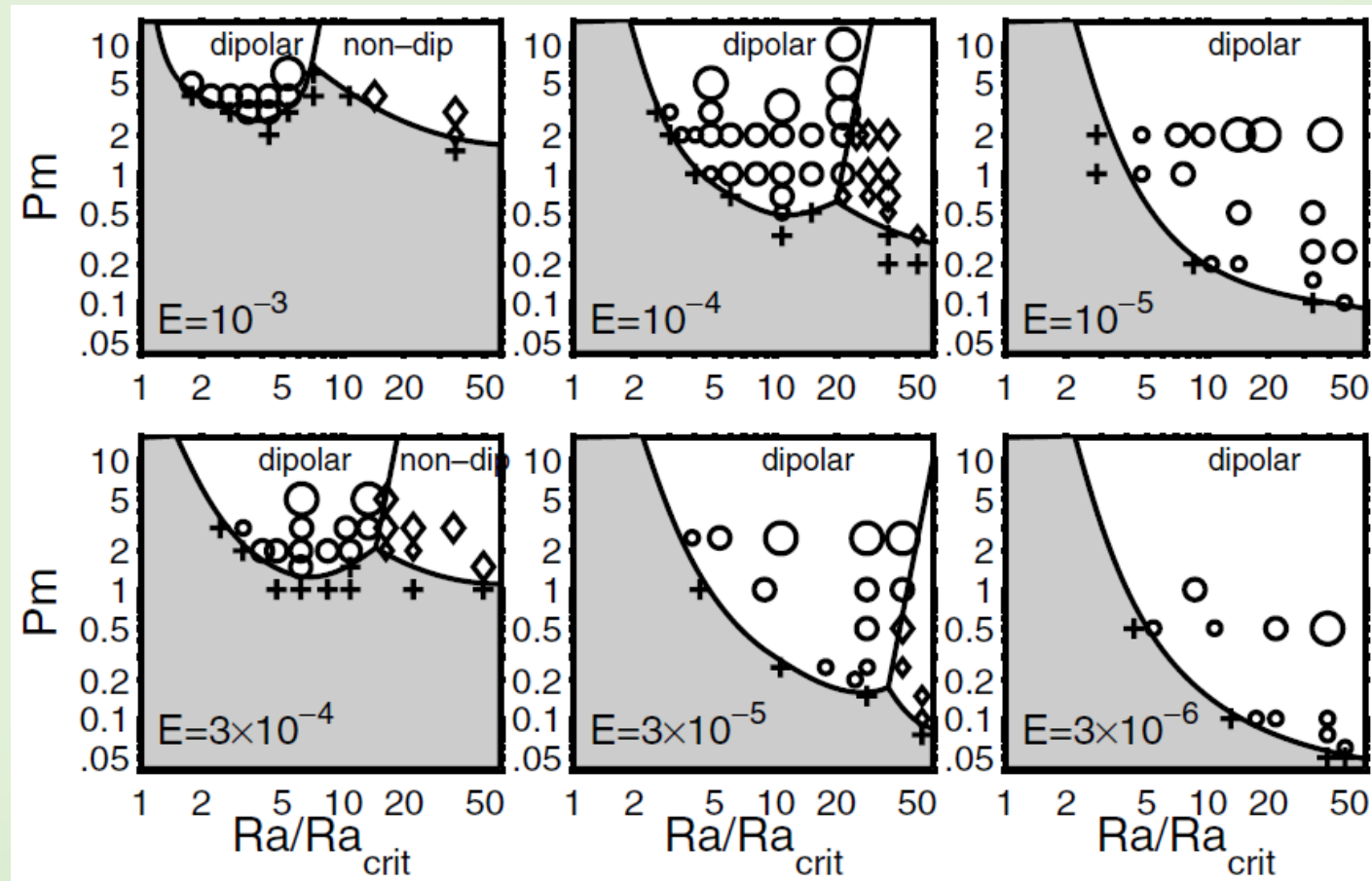
- Thermochemical convection: prescribed CMB flux, fixed ICB temperature, zero co-density sources/sinks.
- No-slip, insulating boundaries.
- For heterogeneous CMB heat an additional parameter  $q^*$

Heat flux Rayleigh	$Ra = \frac{\alpha g_0 q_0 D^4}{\nu k \kappa}$
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Prandtl	$Pr = \frac{\nu}{\kappa}$
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$$q^* = \frac{q_{max} - q_{min}}{2q_0}$$

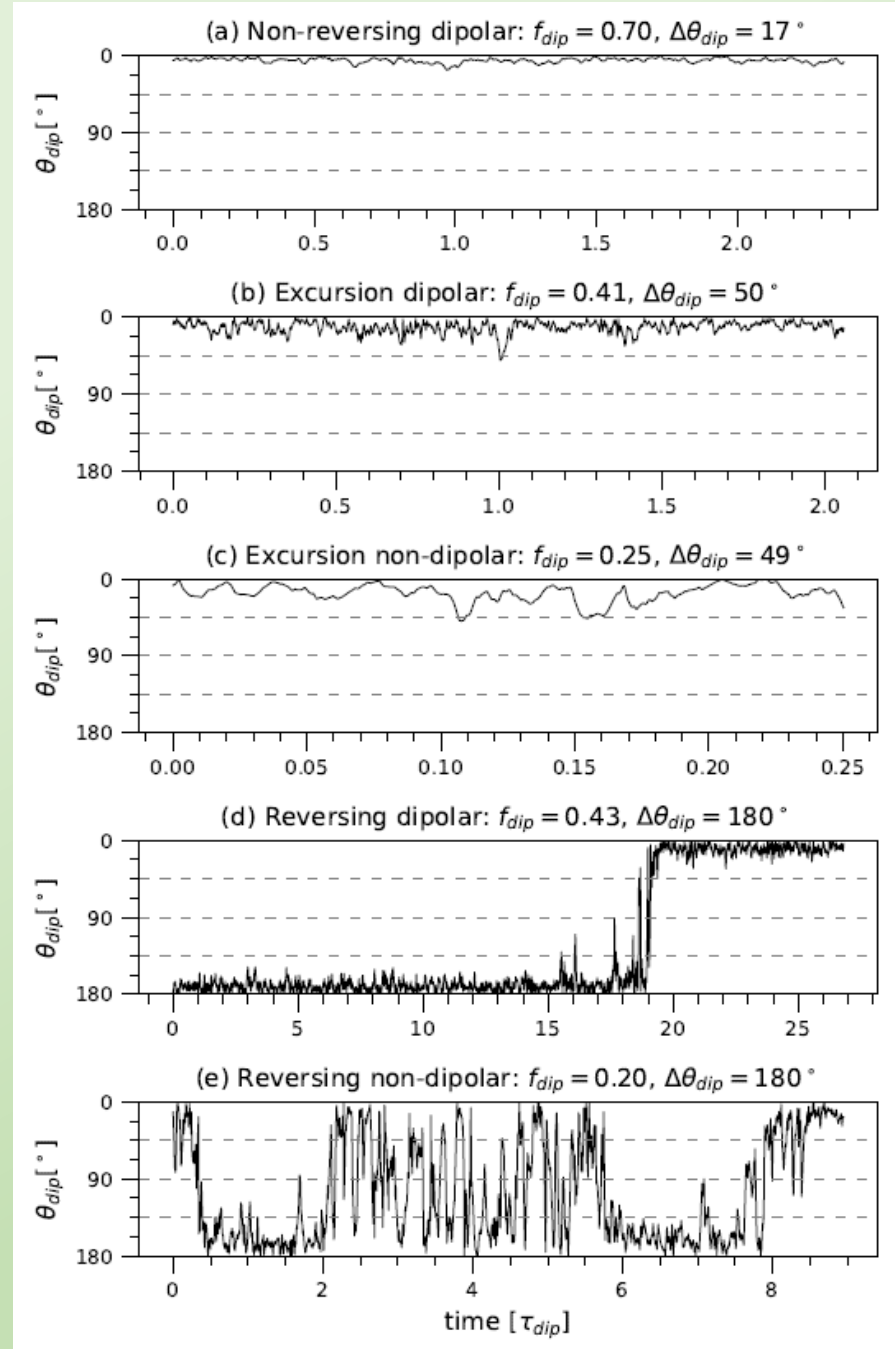
## Dependence on main control parameters - homogeneous boundary conditions



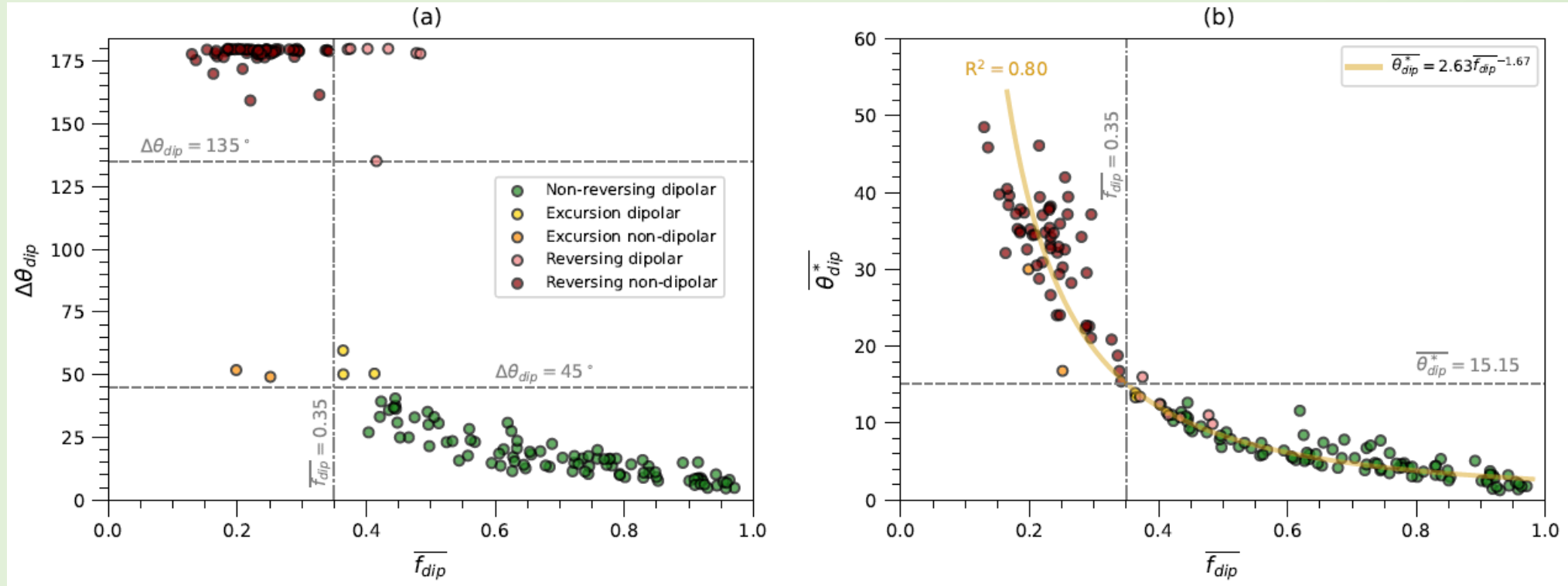
- Transitions (dynamo onset, non-reversing to reversing) established dependencies on main control parameters (e.g. Christensen and Aubert, 2006).
- Dependence on amplitude of CMB heat flux heterogeneity  $q^*$ ?
- Dynamo failure at very large  $q^*$  (Olson and Christensen, 2002)?

## Dynamo models classification

- Dipole tilt range for non-reversing/reversing.
- Critical relative dipolarity for dipolar/multipolar.



# Dynamo models classification



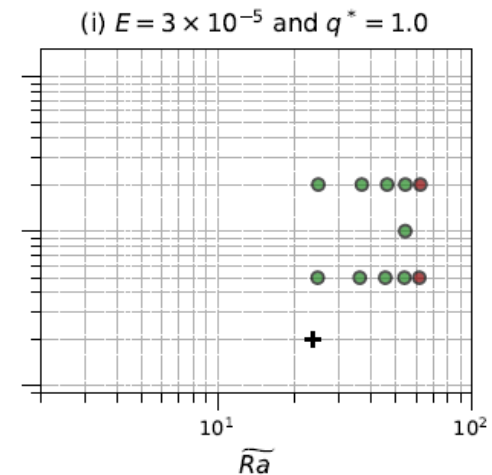
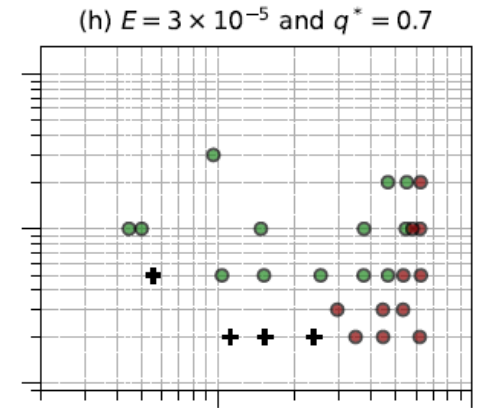
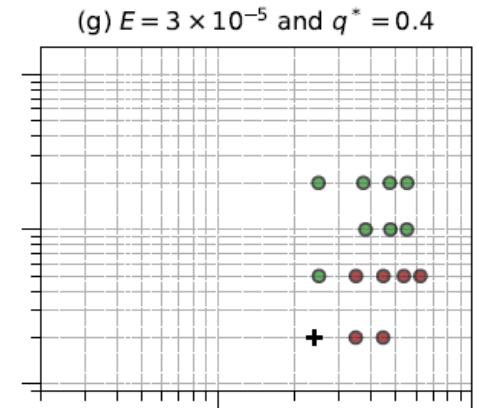
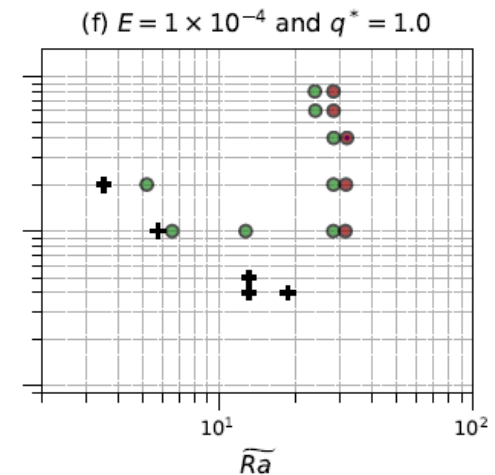
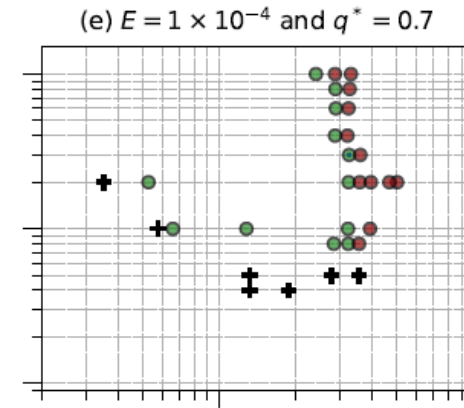
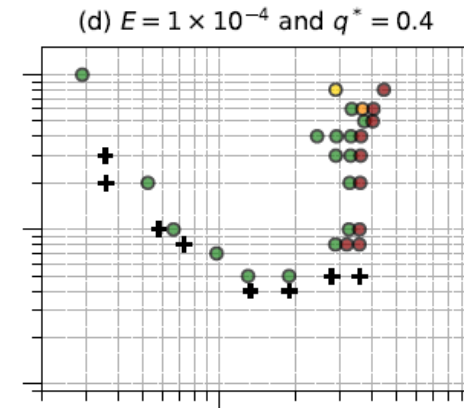
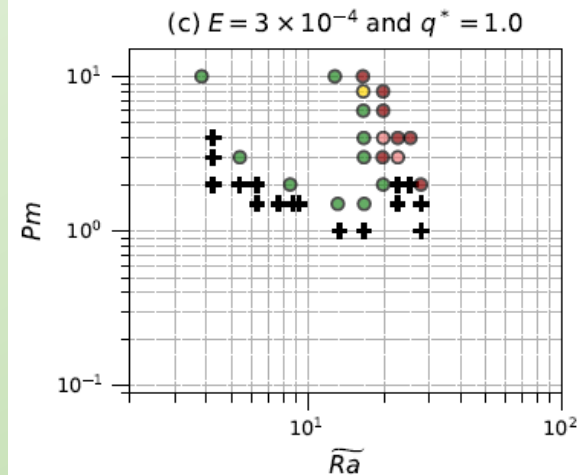
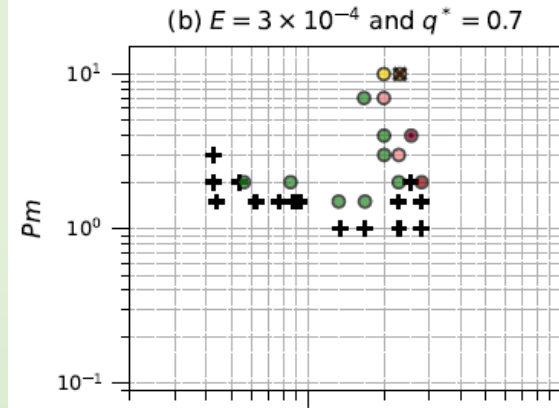
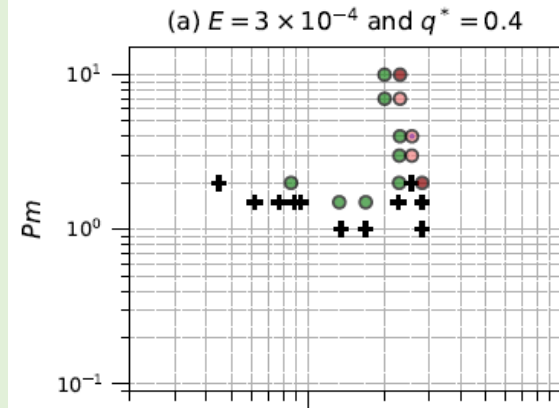
- Dipole tilt range for non-reversing/reversing.
- Critical relative dipolarity for dipolar/multipolar.
- All non-reversing models are dipolar (green).

- Distance of dipole axis from north pole inversely related to relative dipolarity.
- Power law fit intersection with  $\overline{f_{dip}}=0.35 \Rightarrow$  **critical dipole tilt for reversibility.**
- All models above critical dipole tilt exhibit reversals (or excursions) - **predicting reversals** in finite simulation runs.



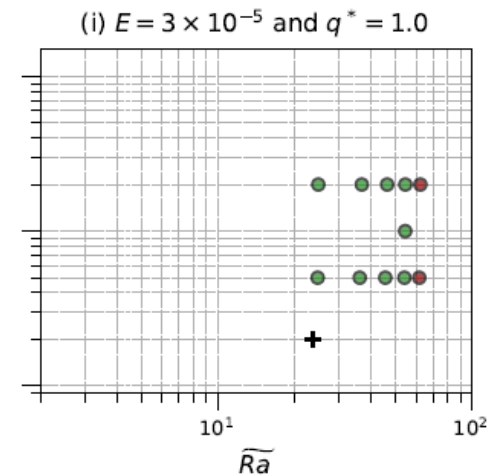
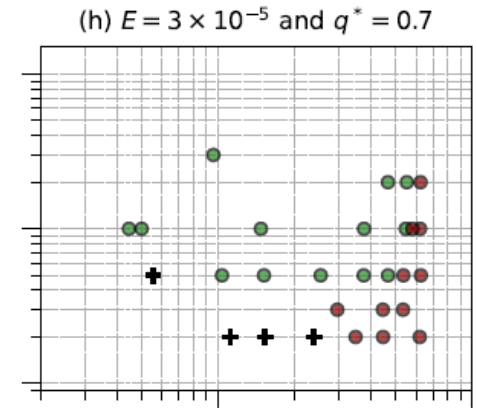
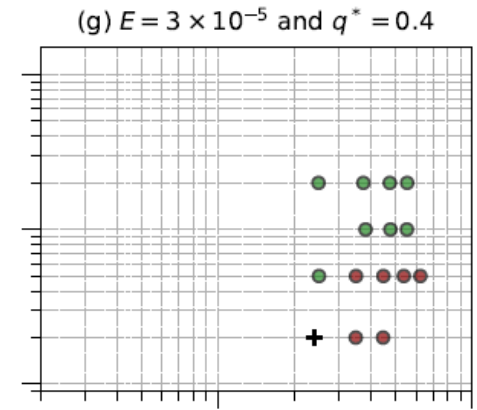
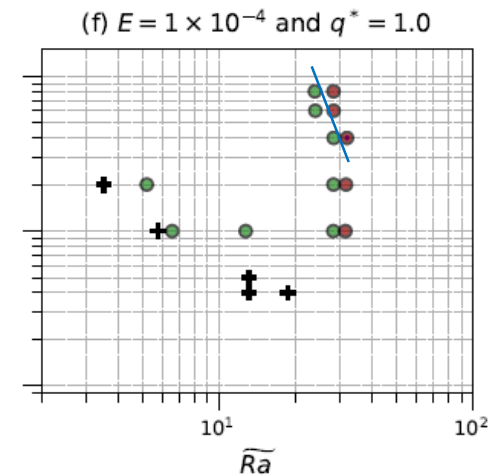
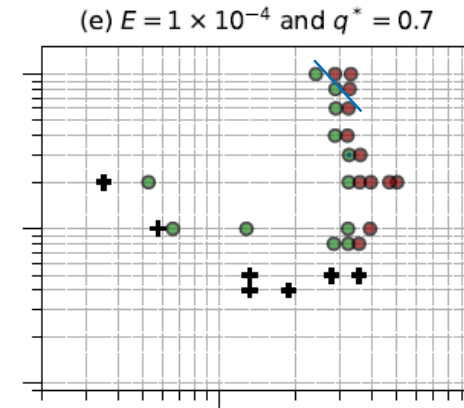
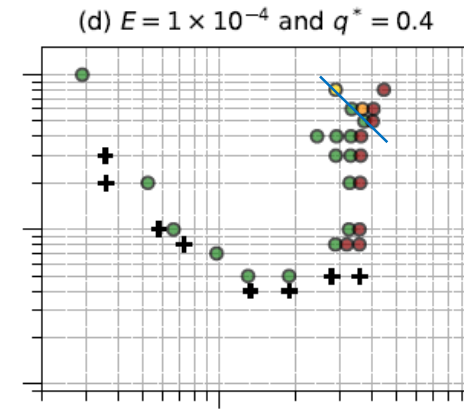
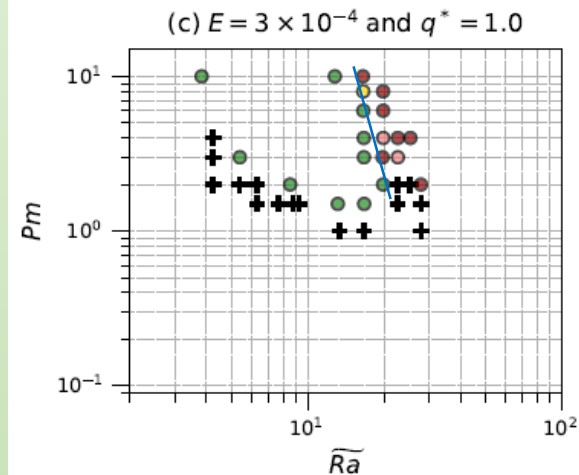
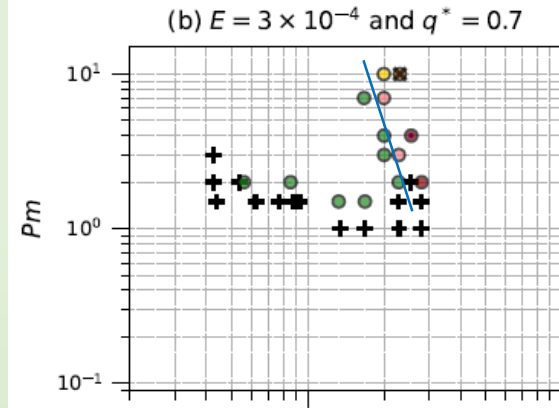
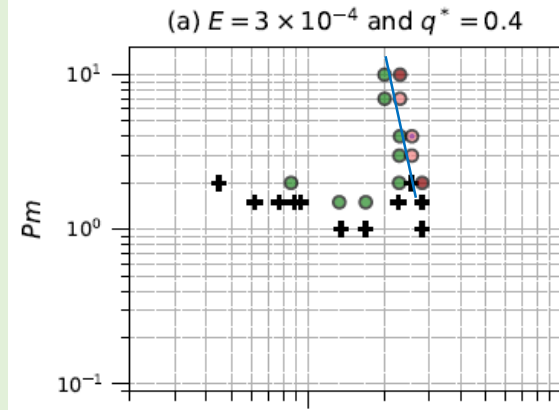
# Dynamo regimes diagrams

- Dynamo regimes vs. convective supercriticality (x-axis) and  $Pm$  (y-axis) for decreasing  $E$  (left to right) and increasing  $q^*$  (top to bottom).
- Increasing convection destabilizes the dipole, increasing rotation rate stabilizes the dipole, as with homogeneous boundary conditions.
- Reversing dipolar models close to the non-reversing/reversing transition.



# Dynamo regimes diagrams

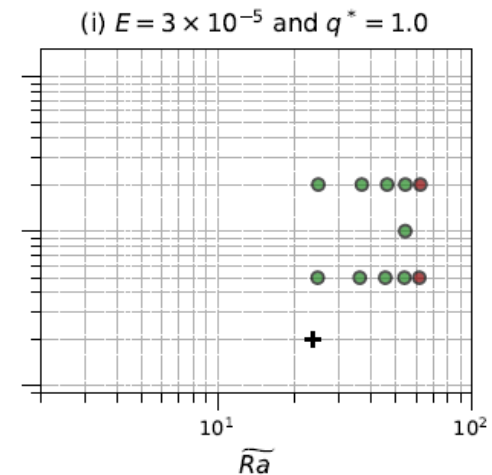
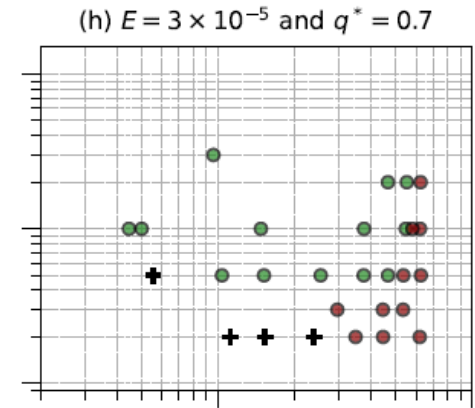
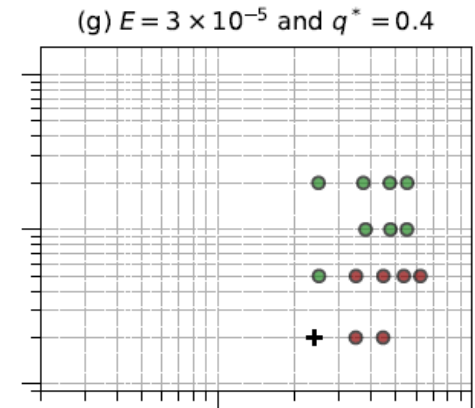
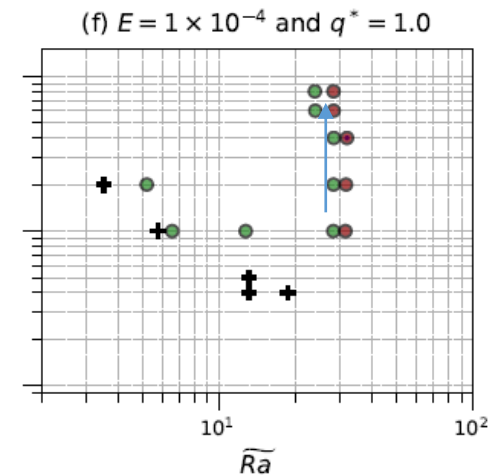
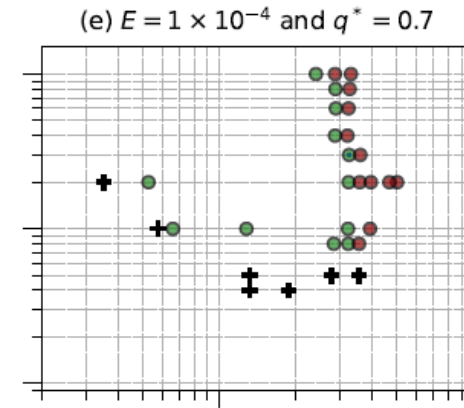
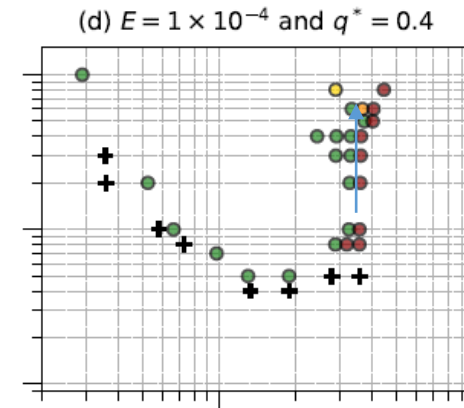
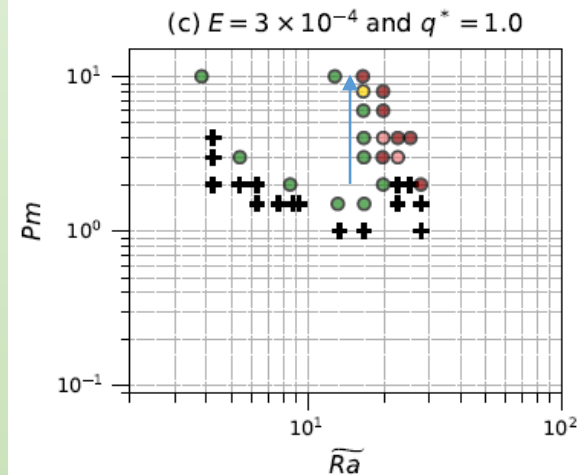
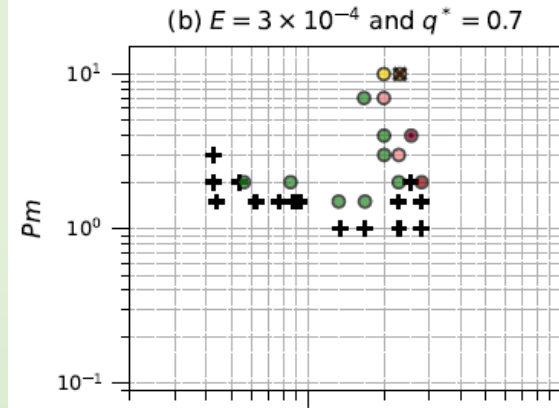
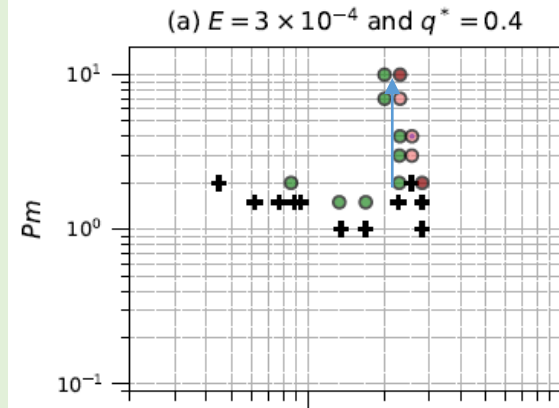
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# Dynamo regimes diagrams

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- Increasing convection destabilizes the dipole, increasing rotation rate stabilizes the dipole, as with homogeneous boundary conditions.
- Reversing dipolar models close to the non-reversing/reversing transition.
- Increasing  $Pm$  destabilizes the dipole (in contrast to dynamos with homogeneous boundary conditions).
- At large  $Pm$  transition to reversals at lower  $Ra$  with increasing  $q^*$  (e.g. a to c or g to i) i.e. boundary heterogeneity favors reversals.



## Dependence on $Ra$

- Transition from non-reversing (a) to reversing (b).

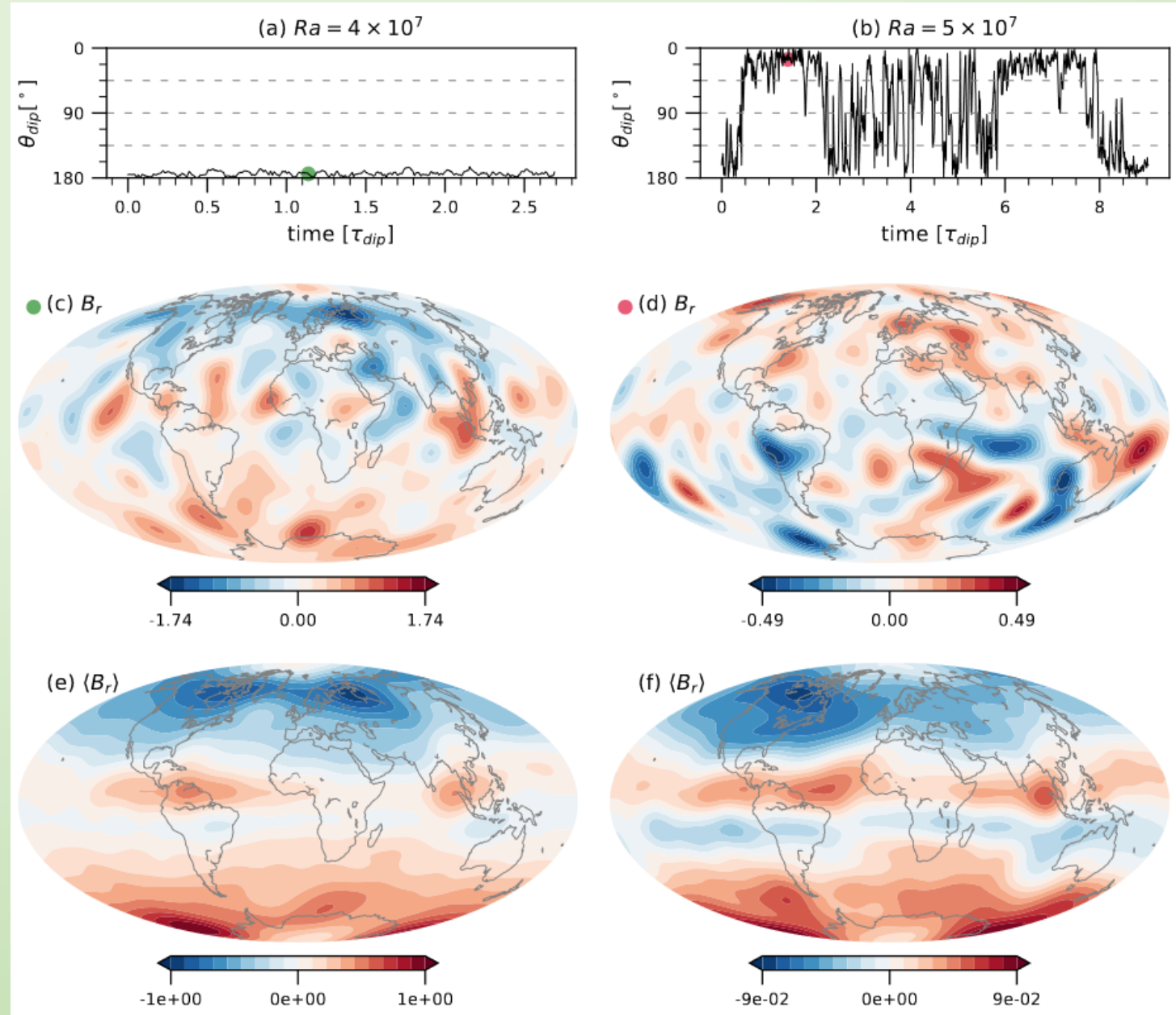
### Snapshots:

- Significant drop in dipolarity (c and d), see e.g. mixed polarities at high latitudes of the southern hemisphere (d).

### Time averages:

- Intense high-latitude flux patches in time-average fields (including reversing case).
- Order 2 signature in non-reversing time-average field, one patch in reversing model.

$$E=1e-4, Pm=2, q^*=1.0$$



## Dependence on $q^*$

- Transition from non-reversing (a) to reversing (b).

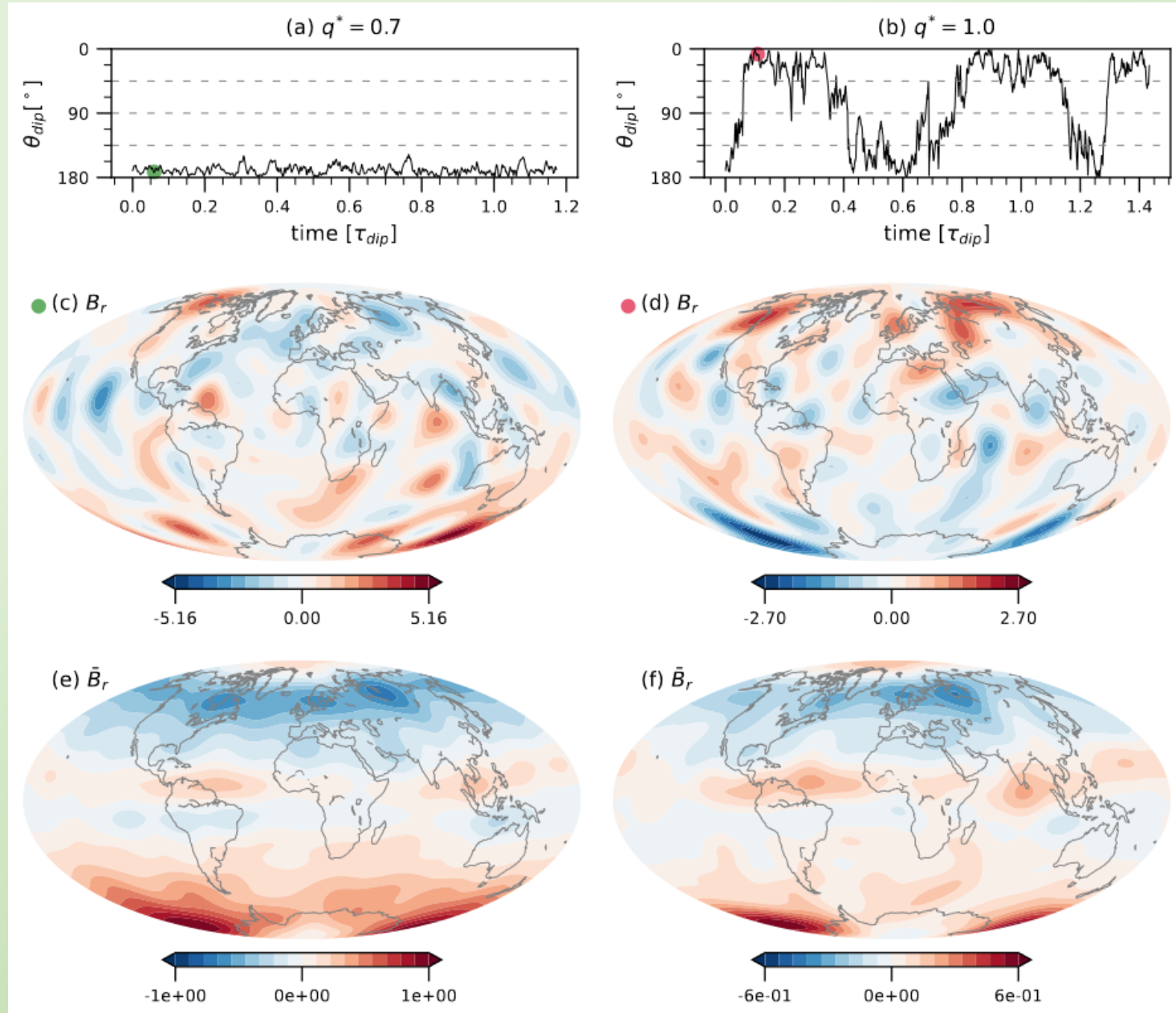
Snapshots:

- Both dipolarities  $>0.35$  (c and d), even slightly larger for the reversing case (d).

Time averages:

- Intense high-latitude flux patches (including reversing case).
- Order 2 signature in non-reversing model, one patch in reversing model.
- Larger amplitude of northern polar minimum (Lézin et al., 2023).

$E=1e-4$ ,  $Ra=4e7$ ,  $Pm=8$



## Dependence on $Pm$

- **Non-trivial transition** from non-reversing (a) to reversing (b).

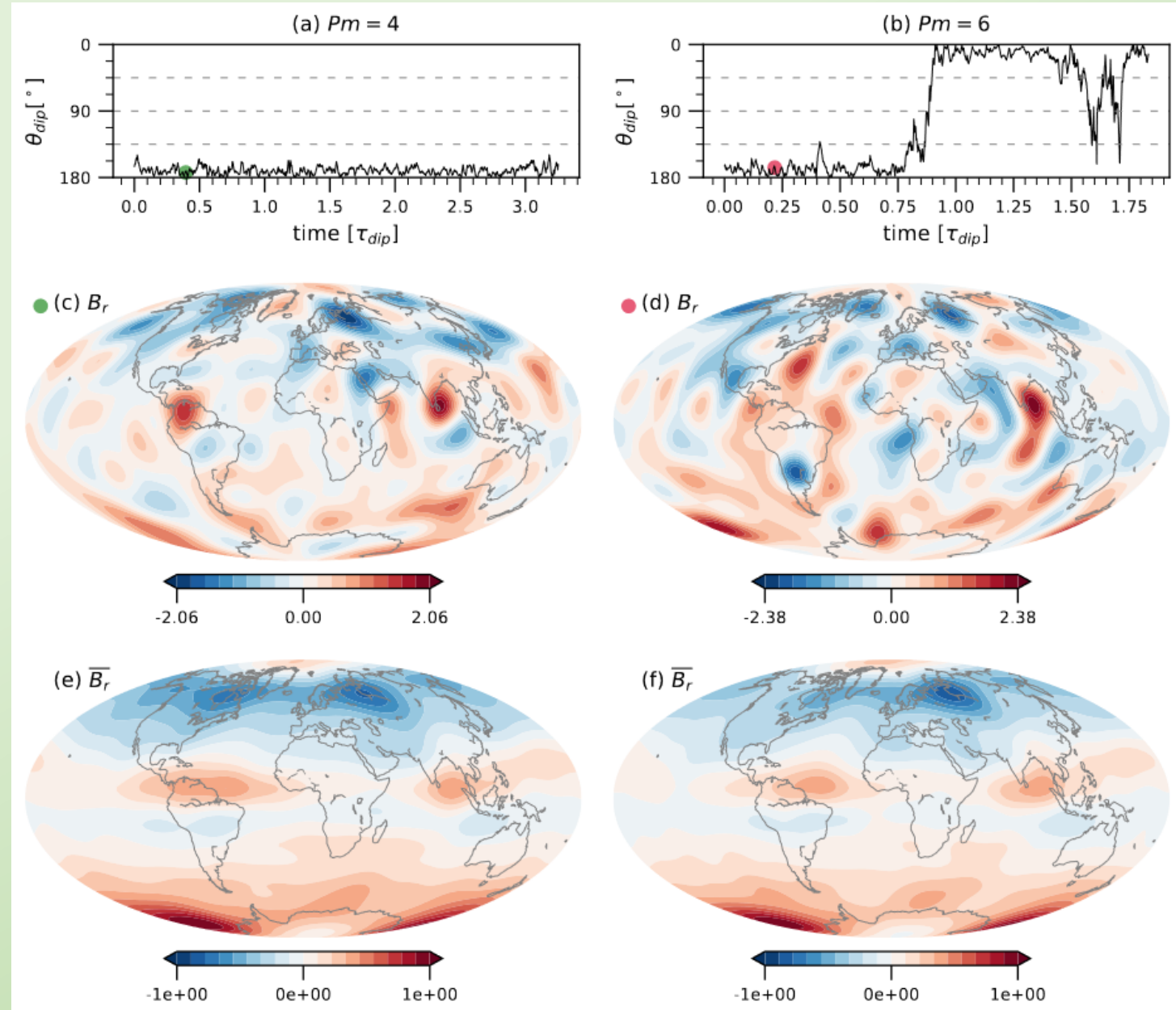
Snapshots:

- Both dipolarities  $>0.35$  (c and d), but significantly lower for the reversing case (c).
- Increasing **boundary-driven equatorially symmetric field** in large  $Pm$  model reduces dipolarity (e.g. below Indian Ocean in d).

Time averages:

- Intense high-latitude flux patches (including reversing case).
- Order 2 signature in non-reversing model, one patch in reversing model.
- Larger amplitude of northern polar minimum (Lézin et al., 2023).

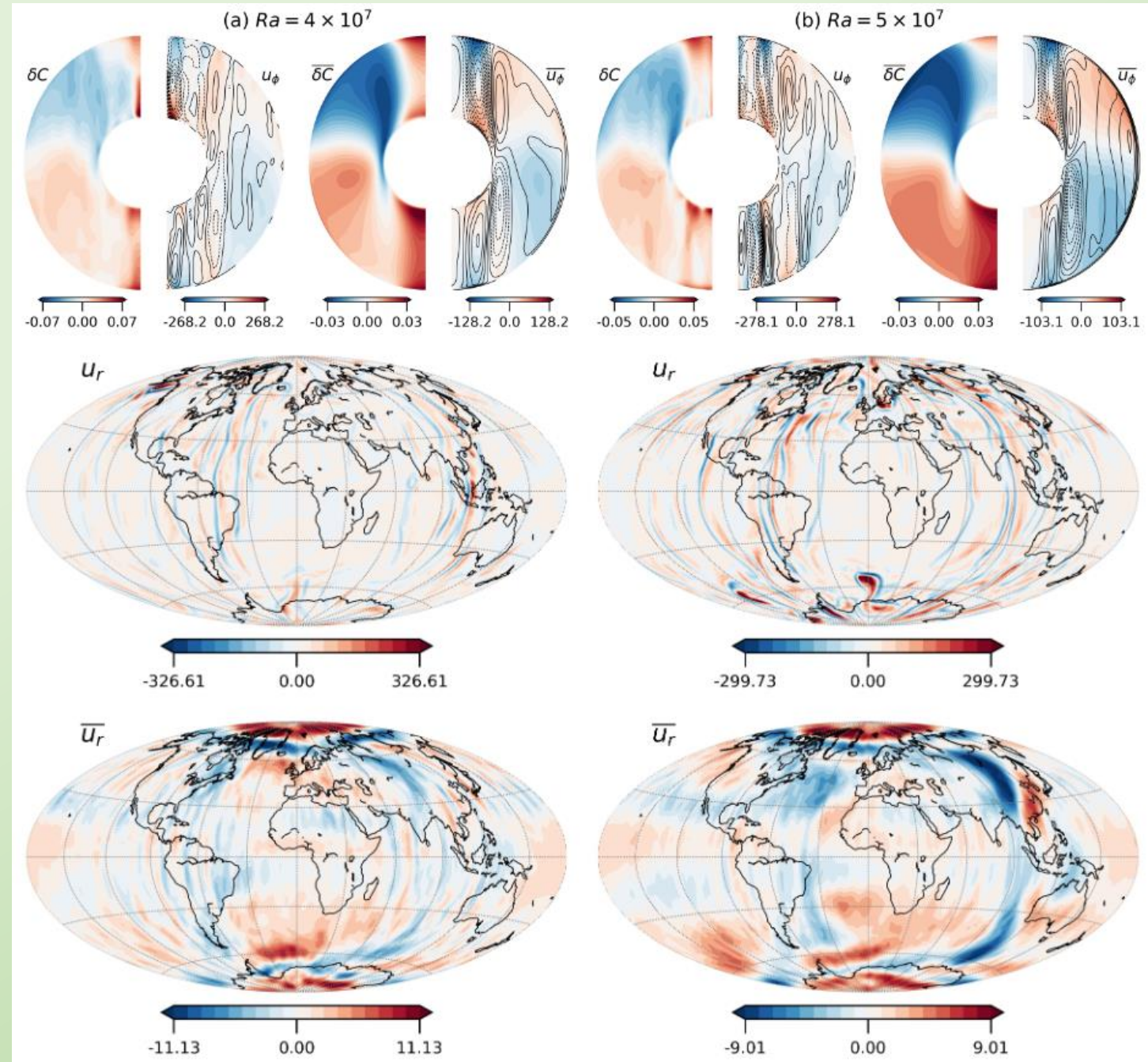
$$E=1e-4, Ra=4e7, q^*=1.0$$





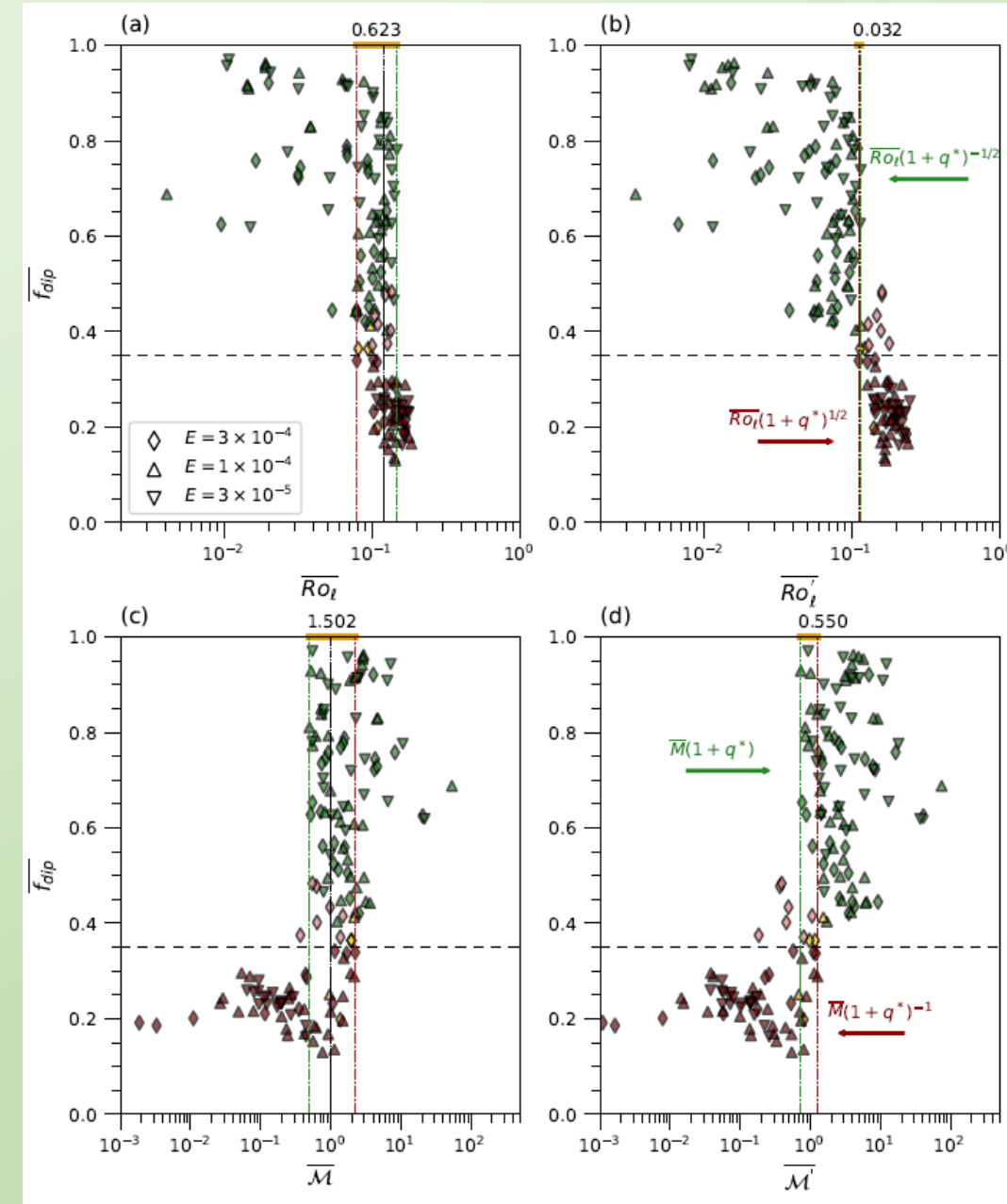
## Dynamical origin

- Dynamics concentrated inside TC in non-reversing model, **more balanced inside/outside TC dynamics** in reversing model.
- Striking **hemispherical co-density** outside TC in both cases driven by southern centers of LLSVPs.
- Strengthening of downwellings below the Americas and east Asia in the reversing model - decreasing role of TC downwellings which maintain the axial dipole (e.g. Christensen et al., 1998) causes reversals.



# Determining parameter for the dipolar to reversing transition

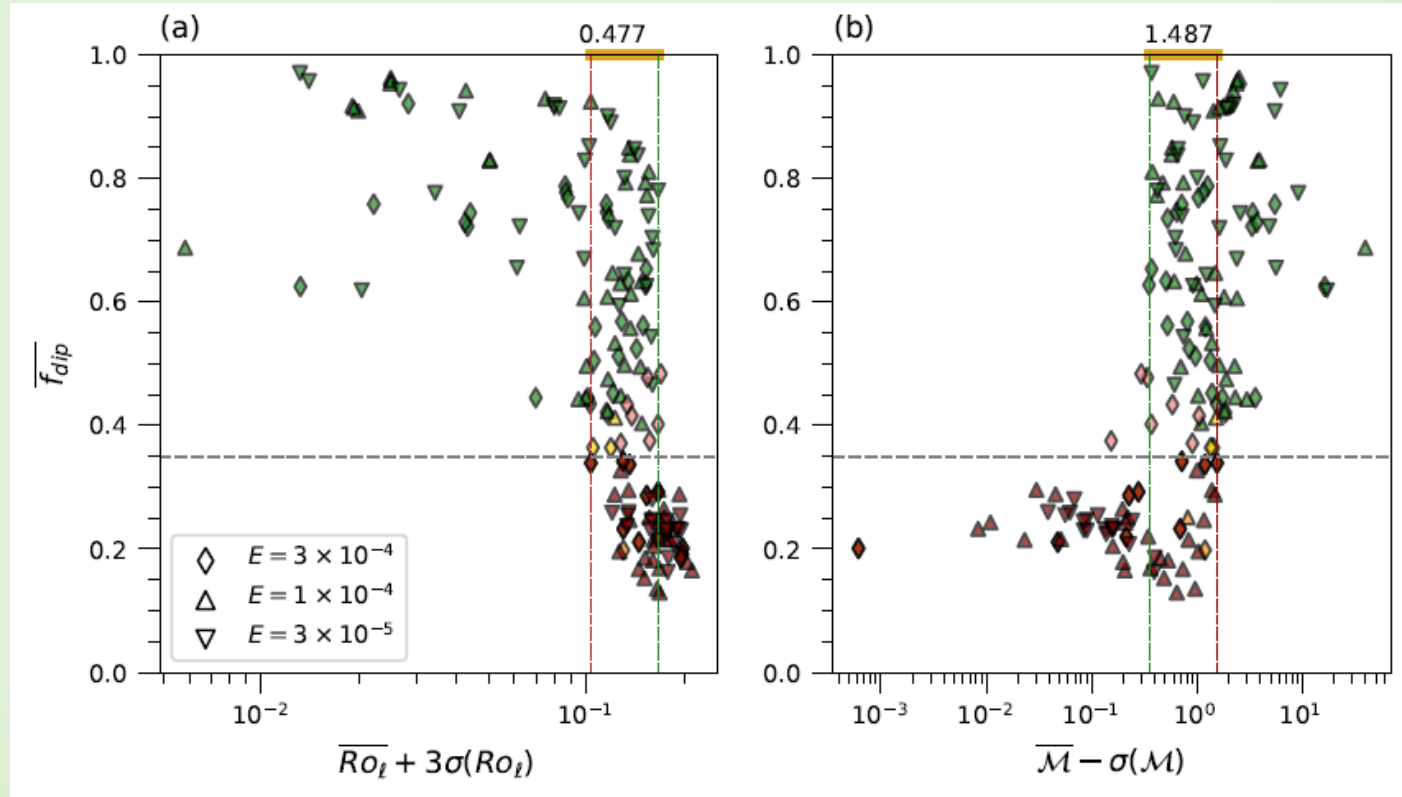
- **Local Rossby number** (Olson and Christensen, 2006) and **magnetic to kinetic energy ratio** (Schwaiger et al., 2019) separate most models but not all.
- **Heterogeneity-corrected** corresponding quantities (Olson and Amit, 2014).
- Increase/decrease in heterogeneity-corrected local Rossby number for reversing/non-reversing dynamos and decrease/increase in heterogeneity-corrected energy ratio for reversing/non-reversing dynamos with increasing  $q^*$ .
- **Inertial control: Regional triggering of reversals** (Terra-Nova and Amit, 2024).
- **Geographical control:** Large heat flux at high latitudes stabilizes the dipole.





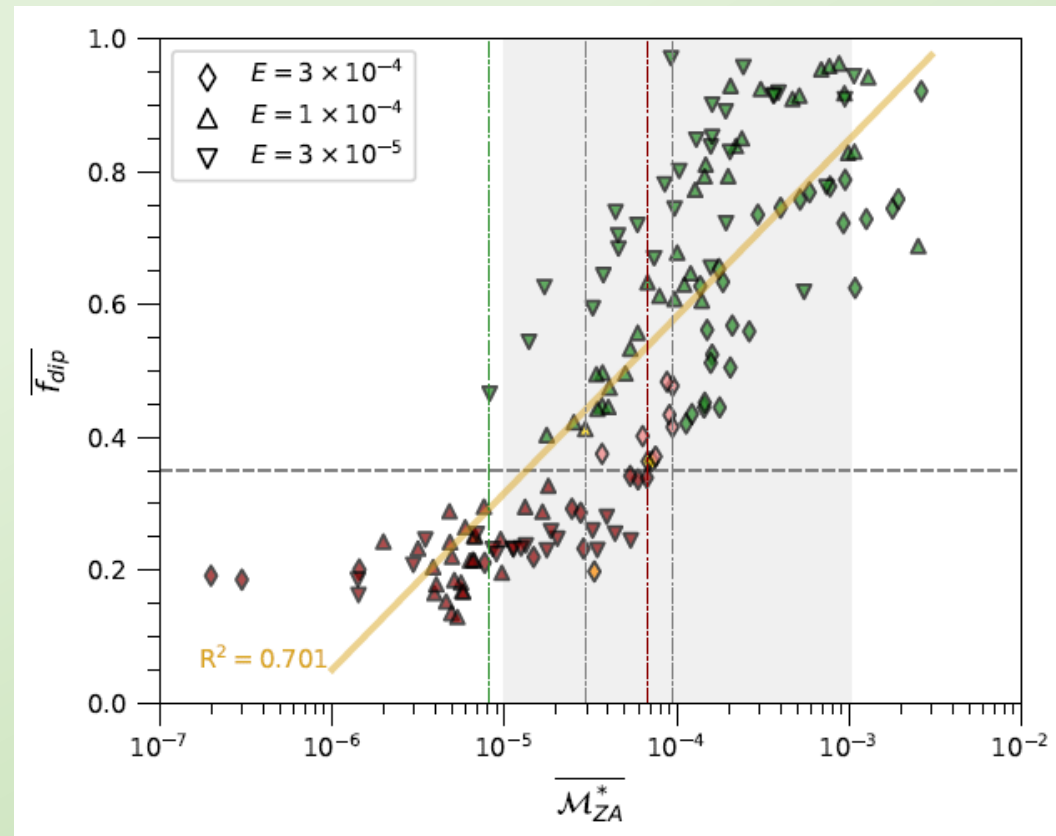
## Determining parameter for the dipolar to reversing transition - temporal variability

Accounting for temporal variability only weakly reduces the overlap for both the local Rossby number and the energy ratio.



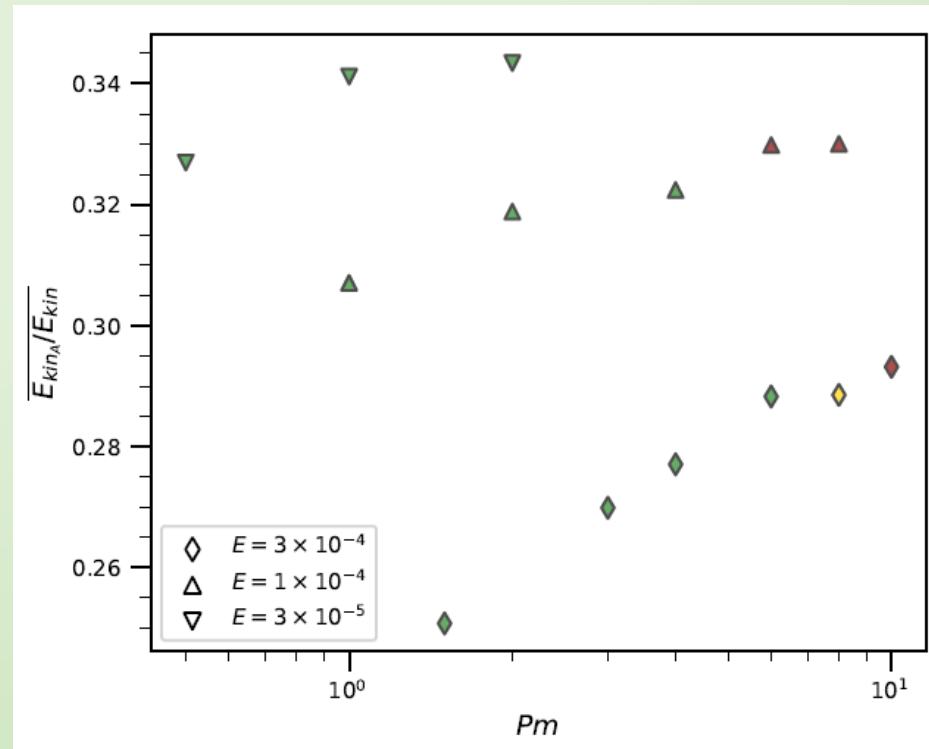
## Determining parameter for the dipolar to reversing transition - equatorial symmetry

- Relative dipolarity linearly related to **modified zonal anti-symmetric energy ratio** (Frasson et al., 2025).
- But still overlap...
- Reversing dipolar and excursions dipolar models confined to a narrower range of modified energy ratios (black vertical lines) than of Frasson et al. (2025) (grey box) - effect of tomographic vs. distinctive outer boundary heat flux patterns.



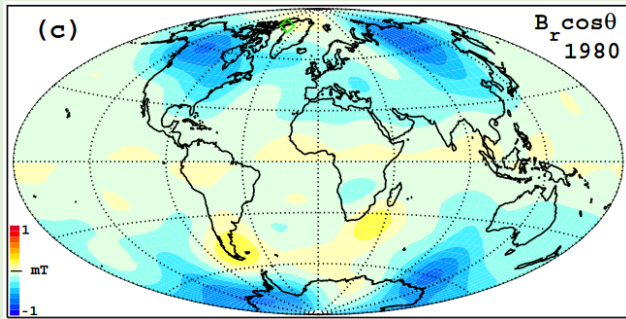
## $Pm$ dependence and boundary-driven equatorially anti-symmetric convection

- Convection = “homogeneous” dynamo + boundary-driven.
- “homogeneous” dynamo: Small-scale (turbulent) equatorially symmetric (rapid rotation effects) convection.
- Boundary-driven: Large-scale mixed symmetric/anti-symmetric (tomographic) convection.
- Increasing  $Pm$  filters small-scale convection (Yadav et al., 2016; Schwaiger et al., 2019) => affects more “homogeneous” dynamo => increase in relative equatorially anti-symmetric convection.

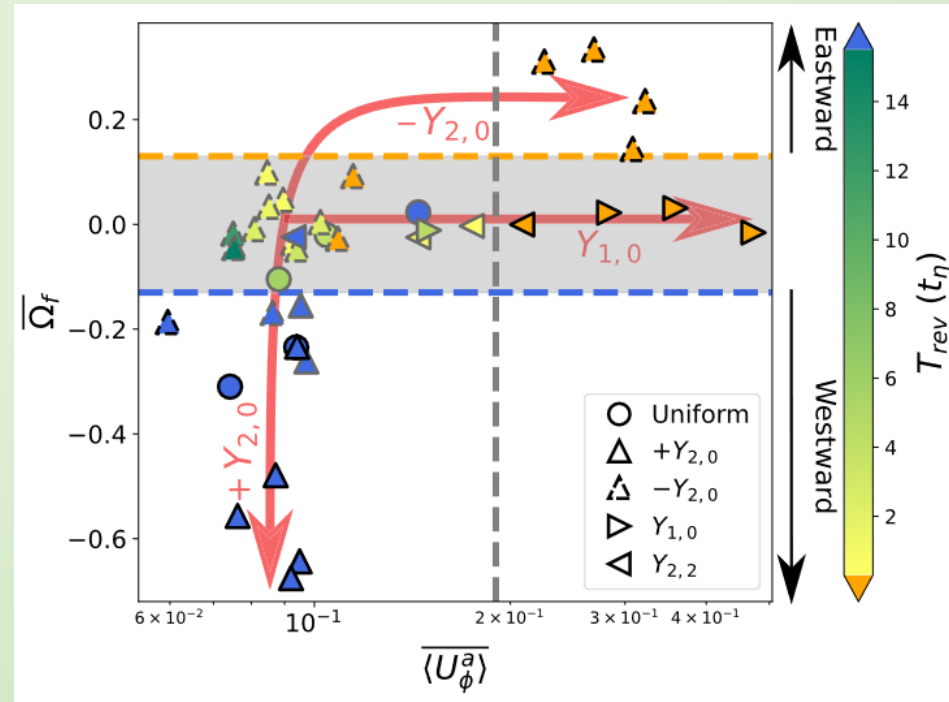


## Discussion - boundary-driven convection inside/outside TC and equatorial symmetry

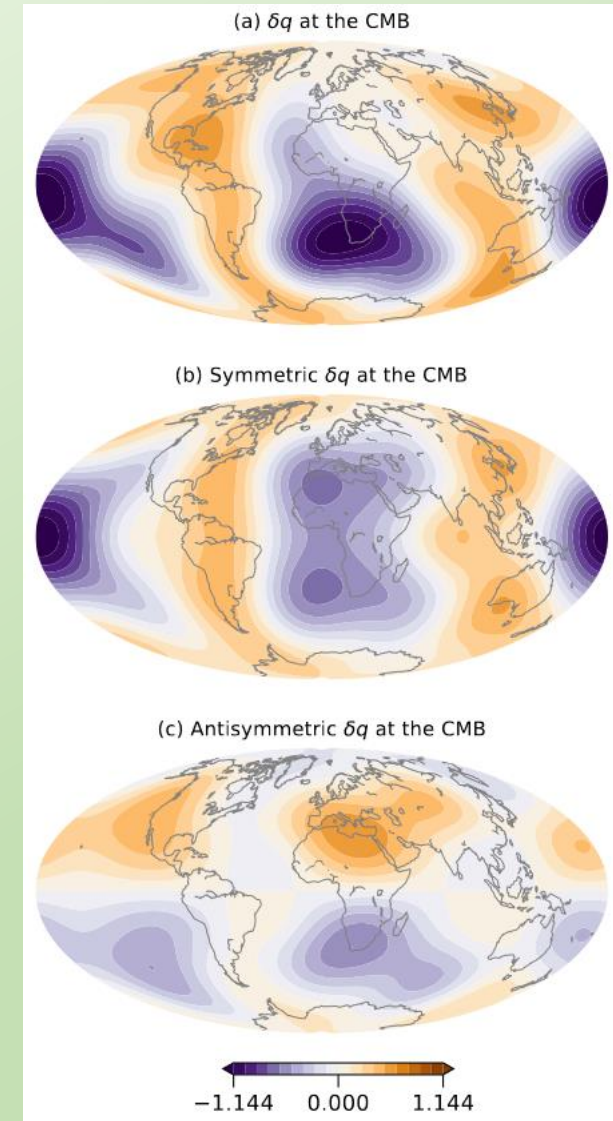
- Axial dipole maintained by intense magnetic flux patches at the edge of the TC.
- Boundary-driven convection outside TC reduces relative intensity of TC downwellings => reversals.
- Boundary-driven anti-symmetric convection => reversals.



Spatial contributions to the geomagnetic axial dipole. From Olson and Amit (2006).



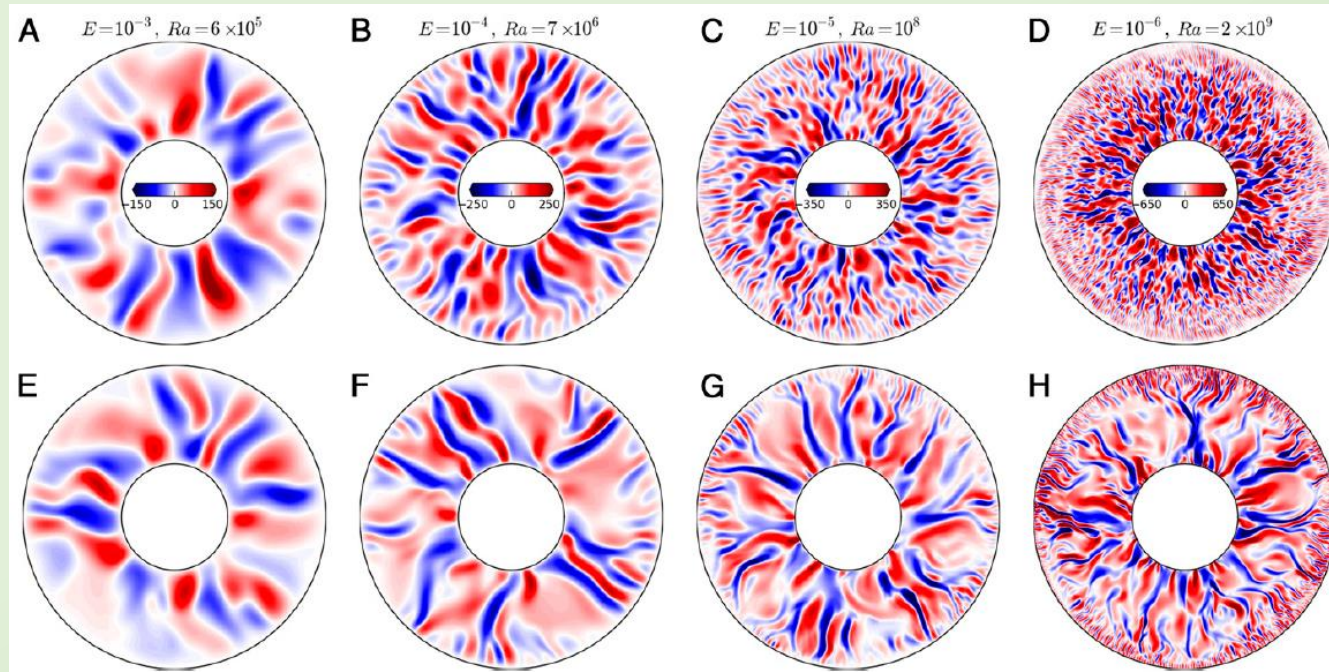
Impact of equatorial symmetry of the flow on the reversibility of dynamo models. From Frasson et al. (2025).



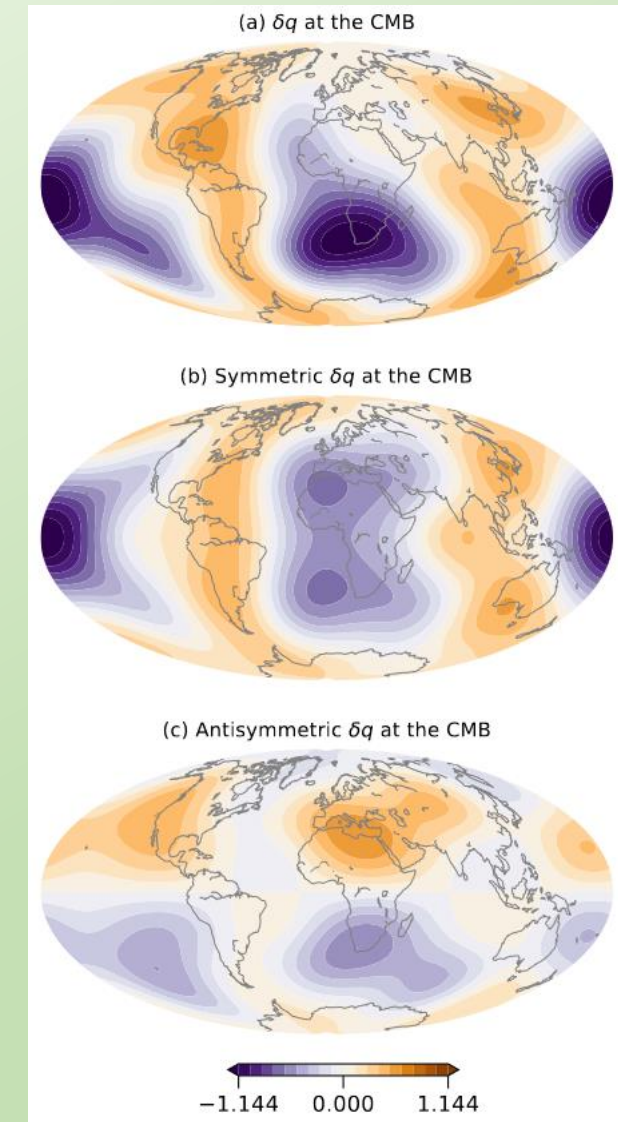


## Discussion - dynamo regimes $Pm$ dependence with tomographic CMB heat flux

- Increasing  $Pm$  **diffuses** small-scale convection (Yadav et al., 2016).
- With homogeneous boundary conditions  $\Rightarrow$  small-scale equatorially symmetric convection.
- With tomographic CMB heat flux  $\Rightarrow$  relatively **large-scale** partly **anti-symmetric** boundary-driven convection.
- Increasing  $Pm$  with tomographic CMB heat flux increases equatorial anti-symmetry of convection  $\Rightarrow$  reversals!



Radial velocity in the equatorial plane for non-magnetic (top) and dynamo (bottom) models. From Yadav et al. (2016).



# Dynamo regimes dependence on the heterogeneous CMB heat flux - conclusions

## Classification and regimes diagrams:

- Dynamo models with a time-average dipole tilt  $>15$  degrees will reverse.
- Increasing  $Ra$  promotes reversals, decreasing  $E$  stabilizes the dipole.
- Increasing  $Pm$  favors reversals! Filtering of small-scale equatorially-symmetric “homogeneous” dynamo convection.
- Increasing  $q^*$  favors reversals for moderate  $q^*$  (Terra-Nova and Amit, 2024).

## Boundary-driven convective morphology:

- Tomographic CMB heat flux increases convection outside TC => reduction of TC downwellings favor reversals.
- Tomographic CMB heat flux induces thermal hemisphericity outside TC => anti-symmetric convection favors reversals.

## Determining parameters for the transition:

- Local Rossby number and magnetic energy ratio separate most non-reversing/reversing dynamo models but some overlap lingers.
- Boundary heterogeneity corrected parameters:
  - **Inertial control:**  $q^*$  dependence indicates regional triggering of reversals.
  - **Geographic control:** Large CMB heat flux at high latitudes stabilizes the dipole.
- Confirmed linear relation between relative dipolarity and modified energy ratio (Frasson et al., 2025), but non-reversing/reversing models still overlap.